

Lecture *Hierarchical Planning*

Chapter: *Introduction to (Non-Hierarchical) Planning*

Dr. Pascal Bercher

Institute of Artificial Intelligence,
Ulm University, Germany

Winter Term 2018/2019

(Compiled on: February 20, 2019)

Overview:

1 Organizational Matters

- Lecture & Exam
- Literature
- Lecture Slides

2 Introduction to Planning

- What is Planning?
- Examples

3 Classical Planning

- The STRIPS Formalism
- State Transition Systems

4 Partial Order Causal-Link Planning

- Partial Plans & Flaws
- Problem Definition
- Relationship of POCL and Classical Solutions



Where and When?

Lecture

Tuesday 14:15 - 15:45 Uhr (O27/R 2202)

Thursday 16:15 - 17:45 Uhr (O27/R 2202)

Exercises

Replace every 4th lecture, see Moodle

Consultation Hours

Right after the lectures and by appointment
`pascal.bercher@uni-ulm.de`



Grades

- Exam gives 6 ECTS if passed.
- Scoring at least 50% of the exercise points improves the exam grade by one step (0.3 or 0.4, respectively).



Exam

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Dates

- The exam may be written or oral, depending on the number of participants.
- Exams: We agree on this *now* or *very soon*.



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They provide more details, but are *not* required.



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They provide more details, but are *not* required.
- Most of the lecture's content is *state of the art!* It is way too recent to be in any textbook.
- The suggested text books and lectures mainly provide detailed explanations as well as examples about the basics.



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- M. Ghallab, D. Nau, P. Traverso: *Automated Planning and Acting*, Cambridge University Press, 2016. (Only a very few pages are on hierarchical planning.)



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- Automated Planning, Susanne Biundo, Ulm University. Slides available upon request. (1/6 chapters is about hierarchical planning.)



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Literature, cont'd III

Planning Research in the Scientific Landscape

Most important planning and AI conferences:

- ICAPS, the Int. Conf. on Planning and Scheduling.
ICAPS is the fusion of two conferences in 2003. Before:
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(AAAI = Association for the Advancement of Artificial Intelligence.)



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Most important AI journals:

- Artificial Intelligence (AIJ, AI Journal).
- Journal of Artificial Intelligence Research (JAIR).



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- IPC, the International Planning Competition. Tracks:



Literature, cont'd IV

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- For a comprehensive list, see:
<http://www.icaps-conference.org/index.php/Main/Competitions>



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- Even after putting the slides online the first time, they might still get updated. Ensure to use the newest version when studying for the exam!



Informal Description

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Planning is the art and practice of thinking before acting.

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Selecting a goal-leading course of action based on a high-level description of the world.



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Just a bit more formally...

Planning is the reasoning process required to generate a *plan* – a sequence of action that transforms a given state of a system into a desired one.



Domain-Independent Approach

- We want to define a large *class of problems*, i.e., a range of different problems with certain properties.
- For these problems there are general problem solvers that can solve *all* possible problems of the respective class.



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 - Verification tools exist that test solutions for their actual correctness (redundant if the planning software is definitely bug-free).



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- Potential inefficiency: a domain-specific solver is most likely more efficient than a domain-independent one.



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Though differences must not always be large as shown in one real-world application: Malte Helmert and Hauke Lasinger. “The Scanalyzer Domain: Greenhouse Logistics as a Planning Problem”. In: *Proc. of the 20th Int. Conf. on Automated Planning and Scheduling (ICAPS 2010)*. AAAI Press, 2010, pp. 234–237



Planning in the Research Landscape

Properties of Planning Tasks

- Goals to achieve versus tasks to accomplish:



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- Many more...



Planning in the Research Landscape, cont'd I

What is being researched?

- Plan generation:



Planning in the Research Landscape, cont'd I

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- Plan generation:
 - Algorithms.



Planning in the Research Landscape, cont'd I

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- Plan generation:
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 - Reductions to other problems.



Planning in the Research Landscape, cont'd I

What is being researched?

- Plan generation:
 - Algorithms.
 - Reductions to other problems.
 - Heuristics.



Planning in the Research Landscape, cont'd I

What is being researched?

- Plan generation:
 - Algorithms.
 - Reductions to other problems.
 - Heuristics.
 - Divide problem into independent sub problems.



Planning in the Research Landscape, cont'd I

What is being researched?

- Plan generation:
 - Algorithms.
 - Reductions to other problems.
 - Heuristics.
 - Divide problem into independent sub problems.
 - Mixed-initiative plan generation with a human.



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What is being researched?

- Plan generation:
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 - Divide problem into independent sub problems.
 - Mixed-initiative plan generation with a human.
- Unsolvable planning tasks:



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- Plan generation:
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- Unsolvable planning tasks:
 - Detect (i.e., prove) the unsolvability.



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 - Detect (i.e., prove) the unsolvability.
 - Provide certificates that serve as verifiable unsolvability proofs.



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- Heuristic search.



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- Heuristic search.
- Complexity analysis.



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- Unsolvable planning tasks:
 - Detect (i.e., prove) the unsolvability.
 - Provide certificates that serve as verifiable unsolvability proofs.
- Heuristic search.
- Complexity analysis.
 - How hard are the problems?



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 - How hard are the problems?
 - What can be expressed by our formalisms?



Planning in the Research Landscape, cont'd I

What is being researched?

- Plan generation:
 - Algorithms. ***(covered in lecture)***
 - Reductions to other problems. ***(covered in lecture)***
 - Heuristics. ***(covered in lecture)***
 - Divide problem into independent sub problems. *(not covered)*
 - Mixed-initiative plan generation with a human. *(not covered)*
- Unsolvable planning tasks: *(not covered)*
 - Detect (i.e., prove) the unsolvability.
 - Provide certificates that serve as verifiable unsolvability proofs.
- Heuristic search. ***(covered in lecture)***
- Complexity analysis. ***(covered in lecture)***
 - How hard are the problems?
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Planning in the Research Landscape, cont'd I

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- Modeling support.



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- Explainable planning.



Planning in the Research Landscape, cont'd I

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- Plan and goal recognition.



Planning in the Research Landscape, cont'd I

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Planning in the Research Landscape, cont'd I

What is being researched?

- Modeling support.
- Explainable planning.
- Plan and goal recognition.
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- Application to real-world settings:



Planning in the Research Landscape, cont'd I

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- Modeling support.
- Explainable planning.
- Plan and goal recognition.
- Plan Repair.
- Application to real-world settings:
 - Plan execution and monitoring.



Planning in the Research Landscape, cont'd I

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- Modeling support.
- Explainable planning.
- Plan and goal recognition.
- Plan Repair.
- Application to real-world settings:
 - Plan execution and monitoring.
 - Convey plans to human users.



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- Application to real-world settings:
 - Plan execution and monitoring.
 - Convey plans to human users.
 - *many more ...*



Planning in the Research Landscape, cont'd I

What is being researched?

- Modeling support. (*not covered*)
- Explainable planning. (***covered if time***)
- Plan and goal recognition. (*not covered*)
- Plan Repair. (***covered if time***)
- Application to real-world settings:
 - Plan execution and monitoring. (***covered if time***)
 - Convey plans to human users. (***covered if time***)
 - *many more ...*



Properties of Planning Systems

- Planning is done offline versus online (versus mixed-initiatively).



Planning in the Research Landscape, cont'd II

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Planning in the Research Landscape, cont'd II

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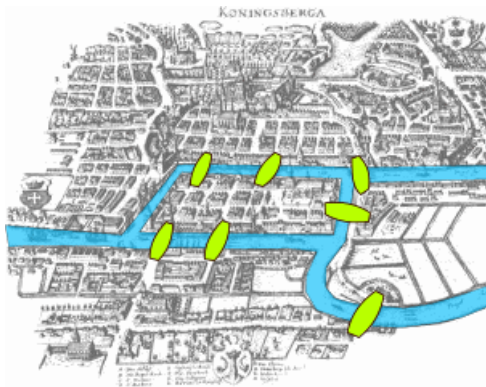
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 - Minimize makespan (time to execute when accounting for parallelism).



Combinatorial Problems, e.g., Seven Bridges of Königsberg



Title: *The Problem of the Seven Bridges of Königsberg*

Source: https://commons.wikimedia.org/wiki/File:Königsberg_bridges.png

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Examples

Riddles, e.g. Dining Philosophers

There are five philosophers, five meals, and five forks.



Picture:

Title: *An illustration of the dining philosophers problem*

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- They all want to have eaten



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Examples

Games, e.g., Solitaire



Source: https://commons.wikimedia.org/wiki/File:GNOME_Aisleriot_Solitaire.png

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Copyright: *Authors of Gnome Aisleriot* <https://gitlab.gnome.org/GNOME/aisleriot/blob/master/AUTHORS>

Examples

Games, e.g., Sliding Tile Puzzle, 15 Puzzle, n^2-1 Puzzle

2	1	4	8
9	7	11	10
6	5	15	3
13	14	12	

Problem



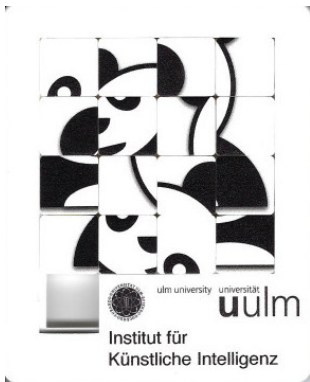
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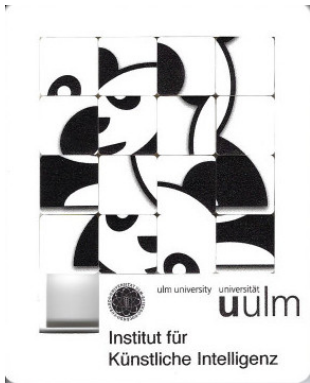


Problem



Examples

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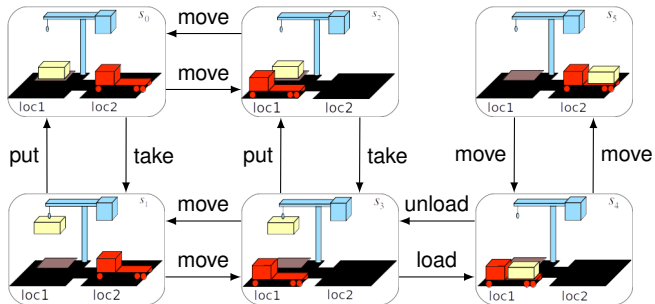
Problem



Solution

Examples

Cranes in a Harbor



Title: Lecture Slides for Automated Planning

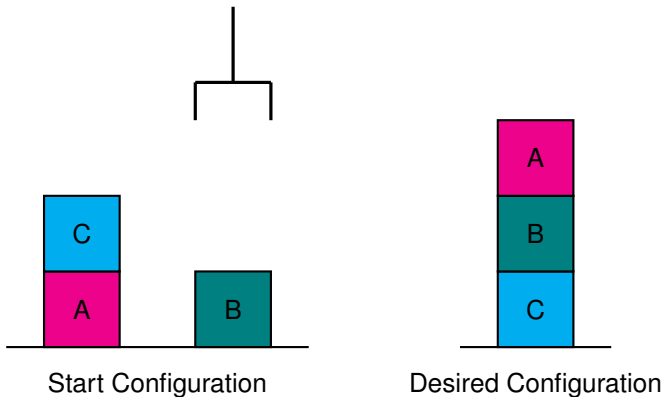
Source: <http://www.cs.umd.edu/~nau/planning/slides/chapter01.pdf>

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Blocksworld

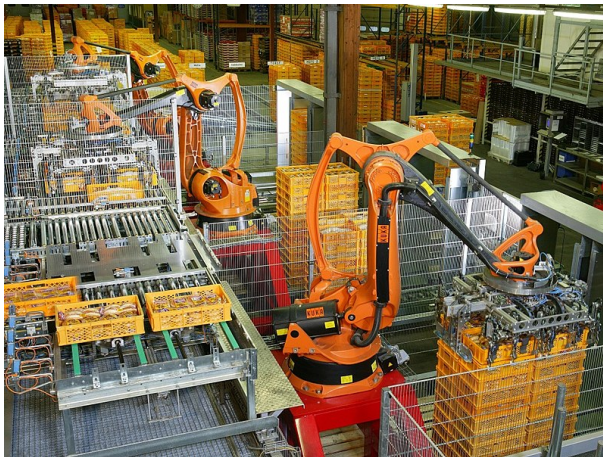


Standard Planning Benchmark in the IPC and *every* planning lecture.



Examples

Automatic Factories, Industry 4.0



Source: https://en.wikipedia.org/wiki/File:Factory_Automation_Robotics_Palettizing_Bread.jpg

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Greenhouse



Source: <https://www.lemnatec.com/>

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Further reading:

- Malte Helmert and Hauke Lasinger. "The Scanalyzer Domain: Greenhouse Logistics as a Planning Problem". In: *Proc. of the 20th Int. Conf. on Automated Planning and Scheduling (ICAPS 2010)*. AAAI Press, 2010, pp. 234–237
- The IPC Scanalyzer Domain in PDDL (see paper above).



Examples

Home Theater Assembly Assistant



Four devices:

- Television (requires video)
- Blu-ray player
- Satellite receiver
- audio/video receiver (requires audio)

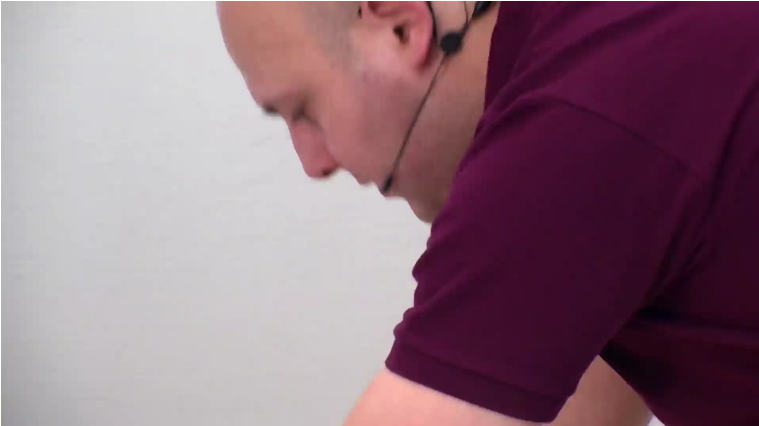
Examples

Home Theater Assembly Assistant, cont'd I (Step-by-Step Instructions)

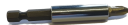
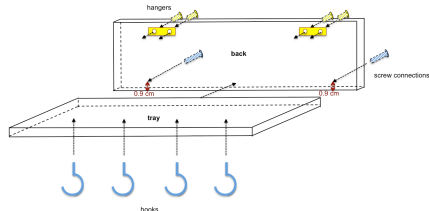


Examples

Home Theater Assembly Assistant, cont'd II (Explanations)



Do-It-Yourself (DIY) Assistant



The material:

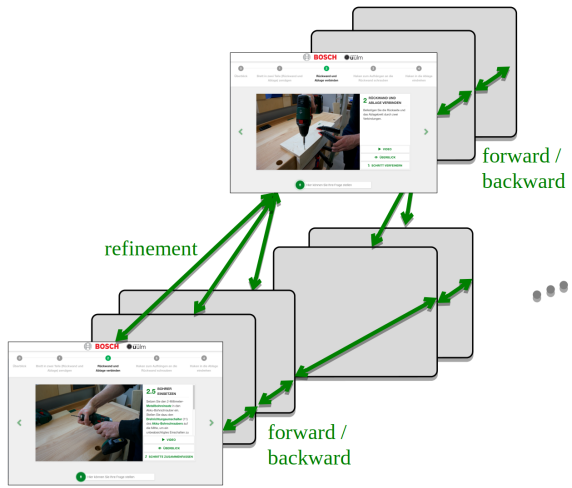
- Boards (need to be cut first)
- Electrical devices like drills and saws
- Attachments like drill bits and materials like nails

Do-It-Yourself (DIY) Assistant, cont'd I (Different Levels of Abstraction)

Presentation of instructions on different levels of abstraction:

Abstract Level

Detailed Level



Examples

Do-It-Yourself (DIY) Assistant, cont'd II (Step-by-Step Instructions)

Logout


0
Überblick

1
Brett in zwei Teile (Rückwand und Ablage) zersägen

2
Rückwand und Ablage verbinden

3
Haken zum Aufhängen an die Rückwand schrauben

4
Haken in die Ablage einziehen



1.1 SÄGEBLATT EINSETZEN

Nehmen Sie gegebenenfalls die Abdeckhaube des **PS1TBL** ab. Ziehen Sie Handschuhe an (Verletzungsgefahr). Schieben Sie die **Sägeblattaufnahme** in Pfeilrichtung nach oben. Schieben Sie das **Holz**sägeblatt mit den Zähnen in Sägeblattaufnahme (sowohl) bis zum Anschlag in die Sägeblattaufnahme. Achten Sie beim Einsetzen des **Sägeblattes** darauf, dass der Sägeblattrücken in der Rolle der **Führungsrolle** liegt und das Sägeblatt fest sitzt.

[▶ VIDEO](#)



[➡ ÜBERBLICK](#)

[⌄ SCHRITTE ZUSAMMENFASSEN](#)

↑ Hier können Sie Ihre Frage stellen

Examples

Do-It-Yourself (DIY) Assistant, cont'd III (Explanations)

Logout

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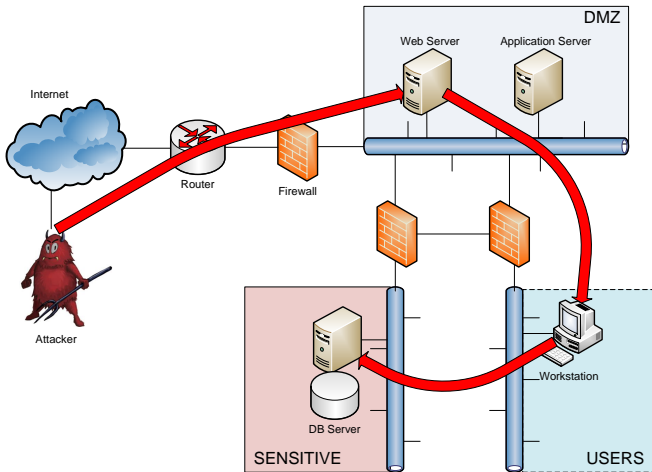
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Examples

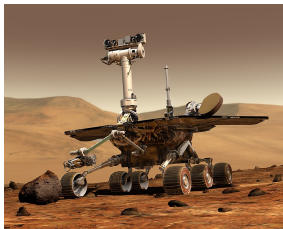
Network Intrusion



Source: <https://fai.cs.uni-saarland.de/teaching/winter17-18/planning-material/planning01-about-this-course-post-handout.pdf>

Examples

Mars Rover



Source: left <https://commons.wikimedia.org/wiki/File:KSC-03PD-0786.jpg>
 middle https://commons.wikimedia.org/wiki/File:Curiosity_Self-Portrait_at_%27Big_Sky%27_Drilling_Site.jpg
 right https://commons.wikimedia.org/wiki/File:NASA_Mars_Rover.jpg

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Further reading: ■ Pascal Bercher and Daniel Höller. "Interview with David E. Smith". In: *Künstliche Intelligenz* 30.1 (2016). Special Issue on Companion Technologies, pp. 101–105. DOI: 10.1007/s13218-015-0403-y
 ■ Every paper about *MAPGEN* (for references, see also article above).

Not Enough?

SiGAPS

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A *solution* (or *plan*) is any sequence of actions transforming the initial state into a goal state.



Historical Remarks

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Today, STRIPS ordinarily refers to (a restricted fragment of) STRIPS' description language.



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- We have only *positive* preconditions, i.e., actions do not pose constraints on what properties do *not* hold in the state of their application.



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- $s_I \in S$ is the initial state (complete state description).
- $g \subseteq V$ is the goal description (encodes a set of goal states).



The STRIPS Formalism, cont'd II

Action application:

- An action $a \in A$ is called *applicable* (or executable) in a state $s \in S$ if and only if $pre(a) \subseteq s$. Often, this is given by a function:
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- If $\tau(a, s)$ holds, its application results into the successor state $\gamma(a, s) = (s \setminus del(a)) \cup add(a)$. $\gamma : A \times S \rightarrow S$ is called the *state transition function*.



The STRIPS Formalism, cont'd II

Action application:

- An action $a \in A$ is called *applicable* (or executable) in a state $s \in S$ if and only if $pre(a) \subseteq s$. Often, this is given by a function: $\tau(a, s) \Leftrightarrow pre(a) \subseteq s$.
- If $\tau(a, s)$ holds, its application results into the successor state $\gamma(a, s) = (s \setminus del(a)) \cup add(a)$. $\gamma : A \times S \rightarrow S$ is called the *state transition function*.
- An action sequence $\bar{a} = a_0, \dots, a_{n-1}$ is applicable in a state s_0 if and only if for all $0 \leq i \leq n-1$ a_i is applicable in s_i , where for all $1 \leq i \leq n$ s_i is the resulting state of applying a_0, \dots, a_i to $s_0 = s_1$. Often, the state transition function is extended to work on action sequences as well $\gamma : A^* \times S \rightarrow S$.



The STRIPS Formalism, cont'd III

Solution:

An action sequence \bar{a} consisting of 0 (empty sequence) or more actions is called a *plan* or *solution* to a STRIPS planning problem if and only if:



The STRIPS Formalism, cont'd III

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- \bar{a} is applicable in s_j .



The STRIPS Formalism, cont'd III

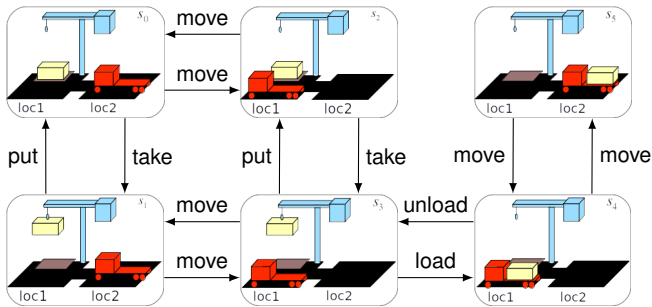
Solution:

An action sequence \bar{a} consisting of 0 (empty sequence) or more actions is called a *plan* or *solution* to a STRIPS planning problem if and only if:

- \bar{a} is applicable in s_I .
- \bar{a} results into a goal state, i.e., $\gamma(\bar{a}, s_I) \supseteq g$.



Example – Exercise!



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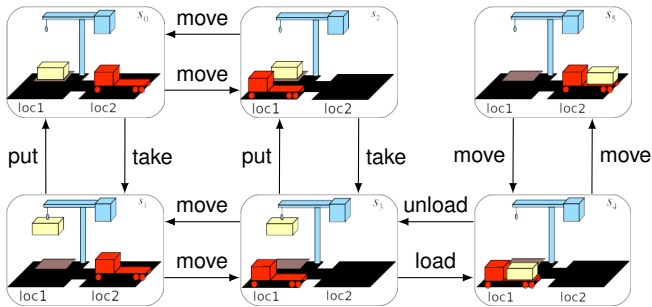
Exercise:

Model a classical planning problem $\mathcal{P} = \langle V, A, s_I, g \rangle$ with the actions and states as indicated above.



The STRIPS Formalism

Example – Exercise!



copyright: see slide 20

STRIPS planning problem:

V : {CrateAtLoc1, HoldCrate, TruckAtLoc1, TruckAtLoc2, CrateInTruck}

A : {take, put, moveLeft, moveRight, load, unload} (see following slides)

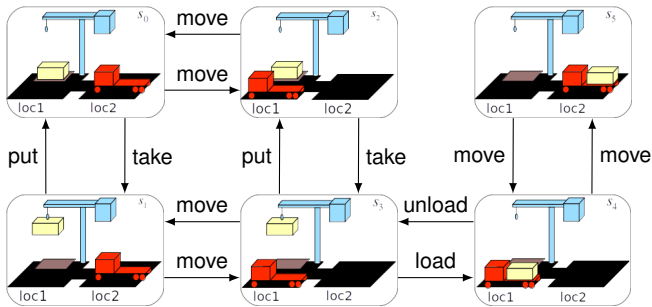
s_i : {CrateAtLoc1, TruckAtLoc2}

g : {CrateInTruck, TruckAtLoc2}



The STRIPS Formalism

Example – Exercise!



copyright: see slide 20

take

pre: {CrateAtLoc1}

add: {HoldCrate}

del: {CrateAtLoc1}

put

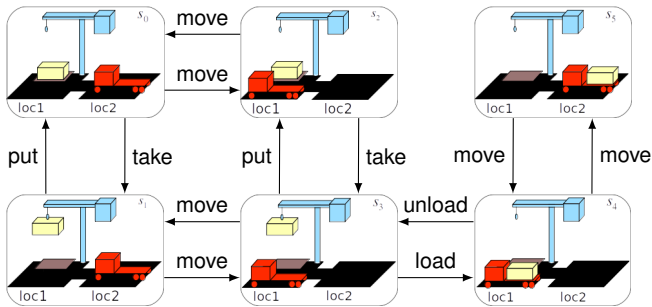
pre: {HoldCrate}

add: {CrateAtLoc1}

del: {HoldCrate}

The STRIPS Formalism

Example – Exercise!



copyright: see slide 20

moveLeft

pre: {TruckAtLoc2}

add: {TruckAtLoc1}

del: {TruckAtLoc2}

moveRight

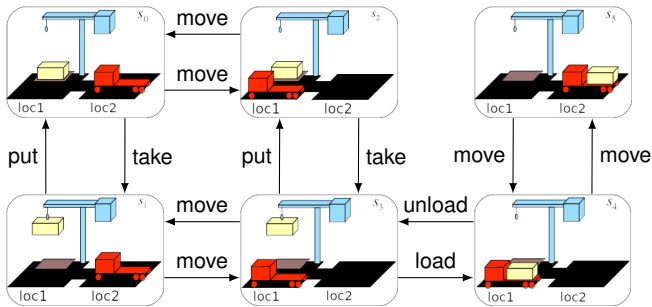
pre: {TruckAtLoc1}

add: {TruckAtLoc2}

del: {TruckAtLoc1}

The STRIPS Formalism

Example – Exercise!



copyright: see slide 20

load

pre: { HoldCrate, TruckAtLoc1 }

add: { CrateInTruck }

del: { HoldCrate }

unload

pre: { CrateInTruck, TruckAtLoc1 }

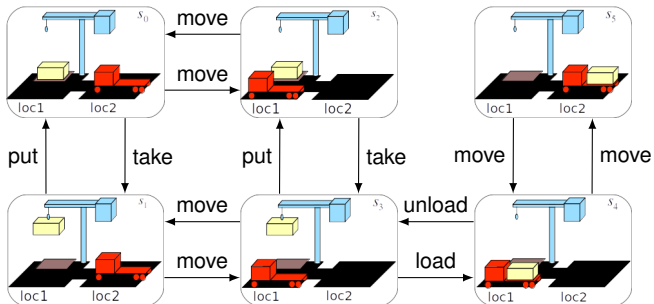
add: { HoldCrate }

del: { CrateInTruck }



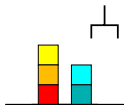
State Transition System

Every classical planning problem is a compact representation of a *state transition system*, i.e., of how states are transformed into each other.



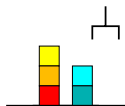
copyright: see slide 20

Size Increase of the State Space in Blocks World



- n blocks, 1 gripper.
- A single action either takes a block with the gripper or puts a block we are holding onto some other block/the table.

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blocks	states	blocks	states
1	1	10	58941091
2	3	11	824073141
3	13	12	12470162233
4	73	13	202976401213
5	501	14	3535017524403
6	4051	15	65573803186921
7	37633	16	1290434218669921
8	394353	17	26846616451246353
9	4596553	18	588633468315403843



State Transition System, cont'd I

Definition (State Transition System)

A state transition system is a 6-tuple (S, L, c, T, I, G) , where

- S is a finite set of states.



State Transition System, cont'd I

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- $I \in S$ is the initial state.
- $G \subseteq S$ is the set of goal states.



State Transition System, cont'd II

Some further terminologies:

- A transition system is called *deterministic* if for all states s and labels l there is at most one state s' , such that $(s, l, s') \in T$. Otherwise, it's called *non-deterministic*.



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- A transition system is called *solvable* if some goal state is reachable.



Questions

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Which of the following transition systems has a *reachable* dead-end?
(We assume that the states of the transition system are *world states*
encoding the respective current situation.)

1 FreeCell?

2 15-Puzzle?

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 - In terms of *causal links* or by checking the linearizations.



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Let $ps = l:a$ be plan step, i.e., l is a label and $a = (pre, add, del)$ an action.



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Let $\prec \subseteq X \times X$ be a strict partial order. Then, a linearization of \prec is a sequence x_1, \dots, x_n of X 's elements that does not contradict the ordering constraints.



Partial Plans (Definition)

Definition (Partial Plan)

Given a planning problem $\langle V, A, s_I, g \rangle$, a *partial plan* is a tuple (PS, \prec, CL) consisting of:

- PS , the finite set of *plan steps*. Each plan step $ps \in PS$ is a pair $l:a$, where l is a *label* (an arbitrary symbol) unique in PS and $a \in A$ is an action.

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 - consists of two plan steps $ps, ps' \in PS$ and a state variable $v \in V$ that occurs both in $add(ps)$ and in $pre(ps')$.
 - implies $(ps, ps') \in \prec$ and there is no ps'' with $ps'' \xrightarrow{v} ps' \in CL$ (unique supporter).

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Recap on Partial Orders

If $\prec \subseteq X \times X$ is a strict partial order, then for all $x, y, z \in X$ holds:

irreflexive not $x \prec x$,
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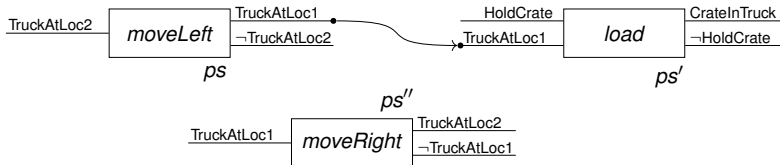
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antisymmetric if $x \prec y$, then not $y \prec x$,
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Example for Causal Links and Causal Threats

Consider the following partial plan from the *Cranes in the Harbor* domain. The causal link $ps \xrightarrow{\text{TruckAtLoc1}} ps'$ documents the achievement of the precondition of ps' by ps .

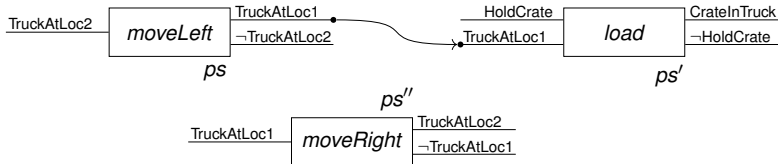


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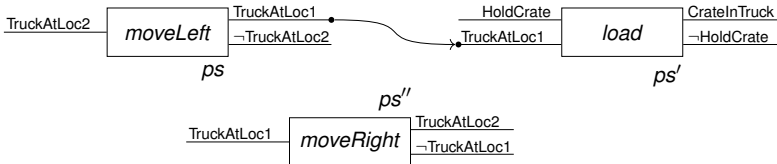
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What can we observe?

- The plan step ps'' is yet unordered with respect to the interval between ps and ps' .
- ps'' could be ordered between ps and ps' .
Thus: it *threatens* the causal link.



Causal Threats

Definition (Causal Threat)

Let (PS, \prec, CL) be a partial plan. A *causal threat* consists of the plan steps $ps, ps' \in PS$, a causal link $ps \xrightarrow{v} ps'$, and the *threatening plan step* $ps'' \in PS$ if and only if



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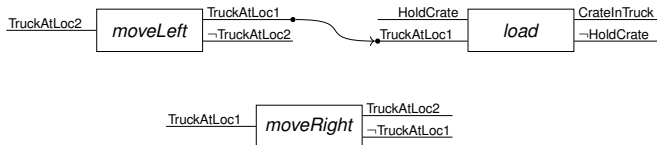
Note:

In case we allow negative preconditions, the definition of causal threats needs to be extended.



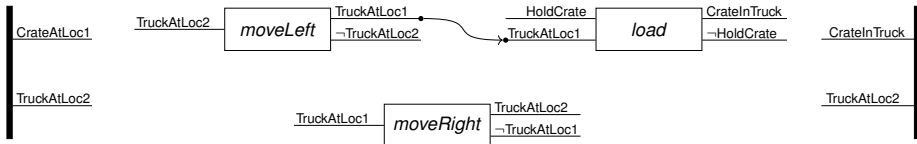
Encoding Initial State and Goal Description

How to represent the initial state and goal description?



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- We represent these states as artificial actions:
 - *Initial State*. For s_I introduce an action $a_I \notin A$ with $pre(a_I) = del(a_I) = \emptyset$ and $add(a_I) = s_I$.
 - *Goal Description*. For g introduce an action $a_g \notin A$ with $pre(a_g) = g$ and $add(a_g) = del(a_I) = \emptyset$.
 - *Ordering Constraints*. Enforce that a_I is the very first action and a_g is the very last.



Encoding Initial State and Goal Description, cont'd

How to represent the initial state and goal description?

- Please note that according to the definition of partial plans (cf. sl. 46) the set of plan steps PS is defined as a set of plan steps $l:a$, where l is a unique *label* symbol and $a \in A$ is an action.



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 - The rest of the definition does not change.



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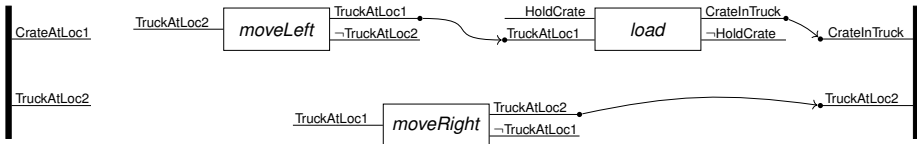
There are two kinds of flaws:

- *Causal Threats* (as defined above).
- *Open Preconditions*. We call a pair (v, ps) consisting of a plan step $ps \in PS$ and its precondition $v \in pre(ps)$ an *open precondition* if and only if there does not exist a causal link $ps' \xrightarrow{v} ps \in CL$.



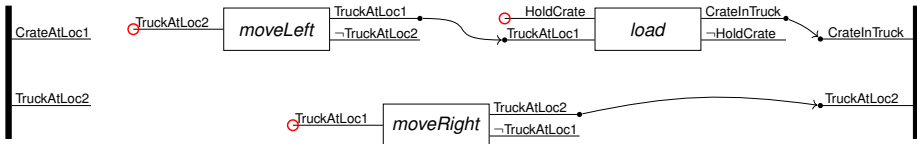
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- Three open preconditions.



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Linearizations of POCL Solutions

Theorem

Let $\mathcal{P} = \langle V, A, P_I \rangle$ be a POCL planning problem with initial state s_I and goal description g . Let $P = (PS, \prec, CL)$ be a plan for \mathcal{P} .

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Exercise!



Linearizations of POCL Solutions, cont'd I

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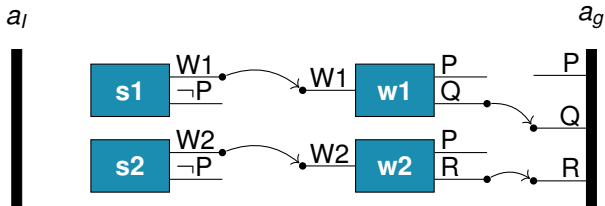
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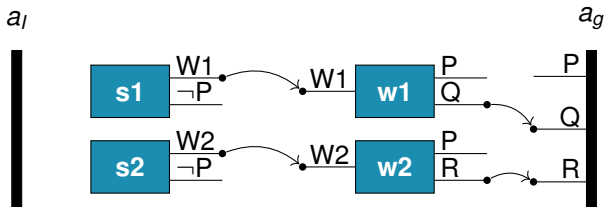
By example (next slide), which was provided by Kambhampati, published by: David McAllester and David Rosenblitt. “Systematic Nonlinear Planning”. In: *Proc. of the 9th National Conf. on Artificial Intelligence (AAAI 1991)*. AAAI Press, 1991, pp. 634–639



Linearizations of POCL Solutions, cont'd II

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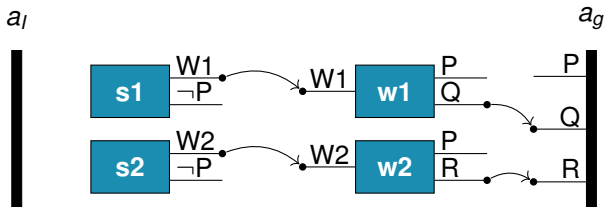
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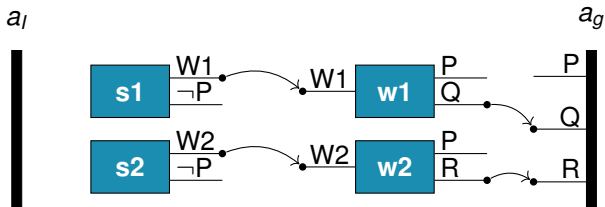
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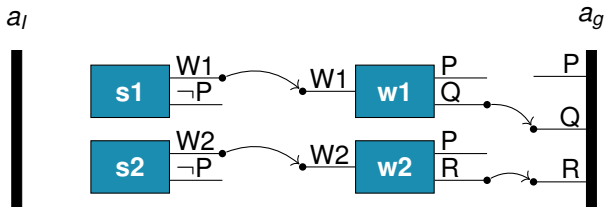
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- However, adding a causal link involving precondition (P, a_g) will introduce a threat and therefore an ordering.



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