# Lecture Hierarchical Planning

# Chapter: Further Hierarchical Planning Formalisms

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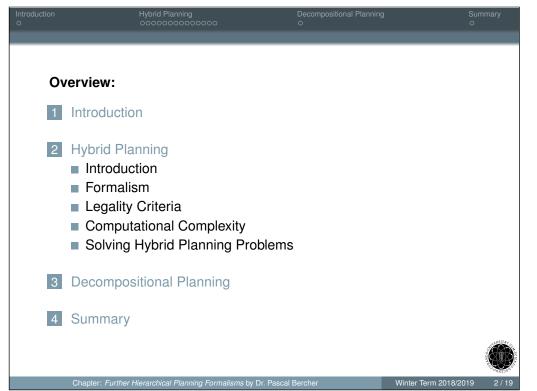
Introduction Hybrid Planning Decompositional Planning Summary

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#### Introduction

- So far, all investigations based upon a simplistic formalization of HTN planning.
- However, there several further hierarchical planning formalisms can be found in the literature.
- Some, we already covered so far:
  - TIHTN planning (covered in detail).
  - A lifted version of HTN and TIHTN planning (introduced rather informally).
  - A lifted HTN planning formalism that allows to express state constraints (briefly mentioned).
- But there are many more:
  - Some regard the task hierarchy advice rather than a restriction. Their goal is to solve classical problems rather than hierarchical ones (but do so hierarchically).
  - Others extend HTN planning to allow modeling support.
  - Others focus on the idea to refine/decompose state features rather than compound tasks.





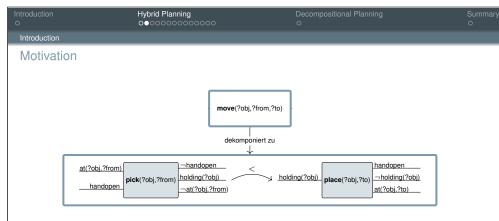
Hybrid Planning Decompositional Planning Summary

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#### Introduction

- Here, we deal with the *problem class* "hybrid planning", not with the *algorithm* hybrid planning!
- To clarify: In the literature, the *Decomposition-based* planning approach (i.e., algorithm) for solving (TI)HTN problems via plan-based search using POCL techniques is also referred to as *hybrid planning* so don't confuse them
- Essentially, hybrid planning (from now on: the problem class!) is the same as (TI)HTN planning problem, but slightly extended:
  - Compound tasks can have preconditions and effects as well.
  - They can be used to define *implementation criteria* they define the circumstances under which a decomposition method is regarded an *implementation* of its compound task.
  - Further, the model (and initial task network) can contain causal links.
  - → Consequently, the solution criteria also involve causal links.





The hybrid planning formalism allows to define preconditions and effects for compound tasks. But why?



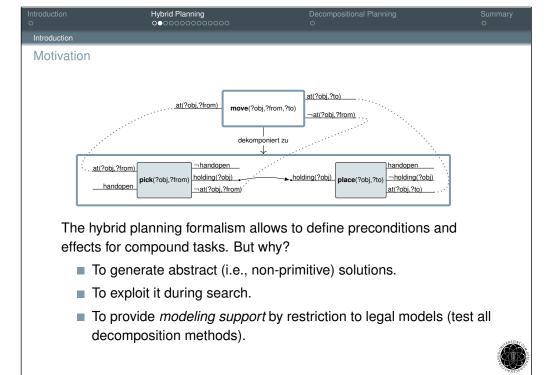
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- Here, we give only a rather informal description of hybrid problems via only mentioning the *differences* to (TI)HTN and POCL problems.
- The problem description extends (TI)HTN problems as follows:
  - Rather than task networks, the model uses partial plans known from POCL planning or from decomposition-based search (i.e., plan steps can be abstract as well and there might be causal links).
  - Compound tasks have the same syntactic form as actions, i.e., they allow for preconditions and effects.
  - Consequently, causal links are allowed to point to or from compound tasks as well.
  - Thus, we need to alter how causal links induce ordering constraints: In contrast to the previous definition (cf. first lecture) only those causal links induce an ordering that are defined between two primitive tasks.







- The solution criteria are essentially the same as for (TI)HTN planning, but extended in two ways:
  - To deal with the causal links pointing to or from a compound task, we demand that upon decomposition they get decomposed to any possible consumer (branching over all possibilities).
  - Solutions are defined as primitive plans without flaws. (Similar to the decomposition-based algorithm.)
- Similar to HTN vs. TIHTN problems, task insertion is an optional property of the the hybrid planning problem class.





- Legality criteria (or implementation criteria) are criteria under which decomposition methods are assumed to be correct (or legal) implementations of their compound task.
- They all try to express "what it means that a compound task has preconditions or effects".
- There are differently strong restrictions, though their theoretical impact is very limited.



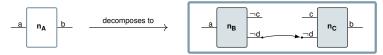
Hybrid Planning

**Downward Compatible** 

# Definition (Downward Compatible, Bercher et al. 2016)

Let  $m = (n_c, P)$  be a method,  $n_c = (pre, eff)$  an abstract task and P a partial plan.

- If  $\varphi \in pre$ , then there exists  $\varphi$  as precondition of a task in P without causal link, which points towards it.
- If  $\varphi \in eff$ , then exists  $\varphi$  as effect of a task in P.



Does this method satisfy the criterion?



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- If  $\varphi \in \mathit{eff}$ , then exists  $\varphi$  as effect of a task in P.
- Prevents/detects the most obvious modeling flaws.
- abstract tasks can always be decomposed as it is the case in standard HTN planning

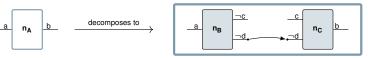


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Does this method satisfy the criterion? Yes!



State-transition Semantics

State-transition Semantics

# Definition (Biundo and Schattenberg, 2001)

Let  $m = (n_c, P)$  be a method,  $n_c = (pre, eff)$  an abstract task, and P a totally ordered plan.

- There needs to be a state s satisfying pre,  $s \models pre$ , such that P's task sequence  $\overline{t}$  is executable in s.
- For all states satisfying the first criterion,  $\bar{t}$  generates a state satisfying *eff*,  $s \models eff$ .
- State-transition semantics adopted to abstract tasks.
- Strong assumption: open preconditions need to be supported by one single state.

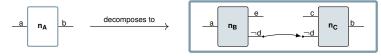


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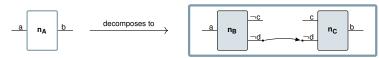


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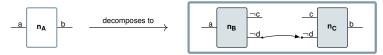


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Does this method satisfy the criterion? No!



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Causal Threat Criterion

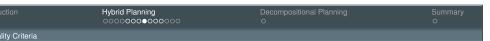
# Definition (Yang, 1990)

Let  $m = (n_c, P)$  be a method,  $n_c = (pre, eff)$  an abstract task, and P a plan.

- pre and eff are actual preconditions and effects in P.
- There are no causal threats.



Does this method satisfy the criterion?



### Causal Threat Criterion

# Definition (Yang, 1990)

Let  $m = (n_c, P)$  be a method,  $n_c = (pre, eff)$  an abstract task, and P a plan.

- pre and eff are actual preconditions and effects in P.
- There are no causal threats.
- Slightly weaker than the last criterion: open preconditions do not need to be achieved by one single state.



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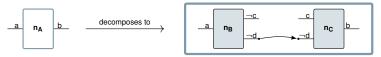
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Does this method satisfy the criterion? Yes!





Causal Link Chain Criterion

# Definition (Young et al., 1994)

Let  $m = (n_c, P)$  be a method,  $n_c = (pre, eff)$  an abstract task, and P a plan.

- $\blacksquare$  Any of  $n_c$ 's preconditions *pre* contributes to at least one of its effects eff via a chain of causal links
- ... and vice versa.
- Neither stronger, nor weaker than the previous criterion.



Hybrid Planning

Legality Criteria

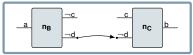
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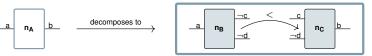


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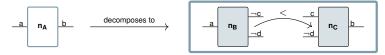


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Does this method satisfy the criterion? No!



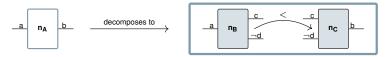
Legality Criteria

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Does this method satisfy the criterion? No!

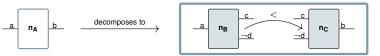


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- ... and vice versa.



Does this method satisfy the criterion?



More than a Name?

- Which impact have the legality criteria on the expressivity?
- lacktriangle We show that every HTN problem  ${\cal P}$  can be transformed into a hybrid planning problem  $\mathcal{P}'$ , such that:
  - $\blacksquare$   $\mathcal{P}$  and  $\mathcal{P}'$  have the same set of solutions (see discussion),
  - $\mathbf{P}'$  satisfies all legality criteria.

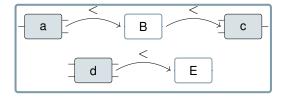




# **Encoding HTN Problems into Hybrid Problems**

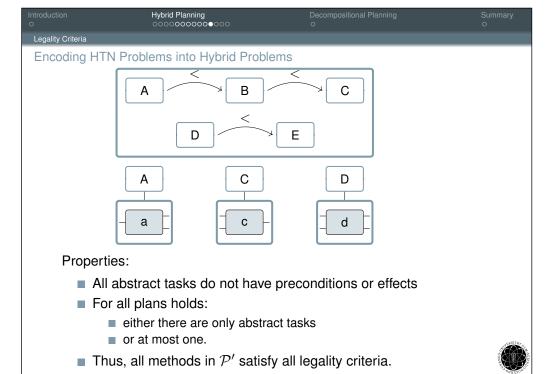
For each primitive task *t*, create an abstract copy *T* without preconditions and effects. Then:

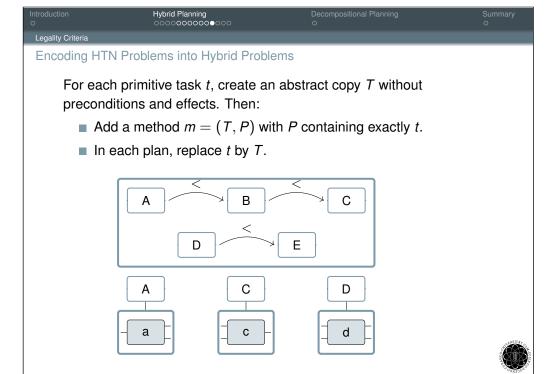
- Add a method m = (T, P) with P containing exactly t.
- In each plan, replace *t* by *T*.

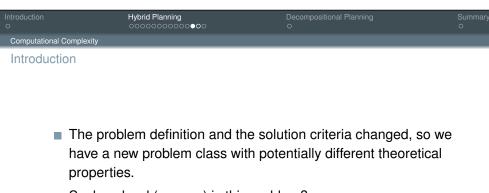




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- So, how hard (or easy) is this problem?
- As we will see: we can express every HTN problem as a hybrid problem without violating any criterion.
- Thus, it's as hard as HTN planning.
- Membership results (lower bounds) are open, but probably identical to those from HTN planning as well.



Computational Complexity

Complexity Results (Plan Existence)

#### Theorem

Hybrid planning is strictly semi-decidable.

#### Proof:

#### semi-decidable:

Perform BFS starting in the initial partial plan.

#### undecidable:

- Reduce the undecidable HTN plan existence problem to hybrid planning
- For this, we use the property shown before, i.e., that every HTN problem can be encoded by a hybrid problem that satisfies *all* legality criteria.



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#### Motivation and Problem Definition

- Decompositional planning was created as a means to reduce search effort for solving classical problems via hierarchical planning techniques.
- That is, it is defined in exactly the same way as *hybrid planning* with task insertion, but without an initial partial plan. Why?
  - Now, also compound tasks can be inserted, which (hopefully) lead to solutions quicker than compared to relying on primitive task insertion completely.
  - Theory-wise, the problem is as expressive as classical planning, because we are not forced to insert compound tasks (and if there is a solution with compound task insertion then there is also one without).



# Hybrid Planning Algorithm

- To solve hybrid problems, we have to use the hybrid planning algorithm (i.e., decomposition-based search), because it's the only one being able to deal with causal links by now.
- That is, as soon as a compilation from hybrid models to standard (TI)HTN models is known, we can again use all standard techniques.
- Reminder: Now, partial plans can already contain causal links. Do we have to change the algorithm? Yes!
  - In some cases, we get fewer successors when decomposing, because we can use the effects of compound tasks as producer (see example from blackboard).
  - When decomposing an abstract task that's involved in causal links, we get, in general, much more successors than it's number of methods (see example from blackboard).



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# Summary

- There are many hierarchical planning formalisms more than just the HTN or TIHTN formalisms discussed so far.
- One of them is hybrid planning, which extends (TI)HTN planning with concepts known from POCL planning.
- Closely related is decompositional planning, which is essentially hybrid planning with task insertion, but without initial partial plan.
- Another formalism is HGN planning, Hierarchical Goal-Task Network planning (we only discussed this briefly).

