

# On the Verification of Totally-Ordered HTN Plans

Roman Barták, Simona Ondrčková  
Faculty of Mathematics and Physics  
Charles University  
Prague, Czech Republic  
{bartak,ondrckova}@ktiml.mff.cuni.cz

Gregor Behnke  
Faculty of Engineering  
University of Freiburg  
Freiburg, Germany  
behnke@informatik.uni-freiburg.de

Pascal Bercher  
School of Computing  
The Australian National University  
Canberra, Australia  
pascal.bercher@anu.edu.au

**Abstract**—Verifying HTN plans is an intractable problem with two existing approaches to solve the problem. One technique is based on compilation to SAT. Another method is using parsing, and it is currently the fastest technique for verifying HTN plans and the only technique supporting state constraints. In this paper, we propose an extension of the parsing-based approach to verify totally-ordered HTN plans more efficiently. This problem is known to be tractable if no state constraints are included, and we show theoretically and empirically that the modified parsing approach achieves better performance than the currently fastest HTN plan verifier when applied to totally-ordered HTN plans.

**Keywords**—hierarchical planning, HTN, verification, parsing, total-order

## INTRODUCTION

Plan verification is about finding if a given action sequence forms a correct plan according to a given planning domain model. For classical plans, the verification problem consists of checking if the action sequence is executable starting with the initial state and checking if the goal condition is satisfied in the final state [1]. For hierarchical plans, plan verification additionally requires that the action sequence can be obtained by decomposition of some task. A specific root task, which decomposes to the action sequence, might also be given to describe the goal task.

There exist two approaches to hierarchical plan verification. One uses a translation of the verification problem into a Boolean satisfiability problem [2]. The second uses parsing and it supports state constraints [3], [4]. The hierarchical planning domain model can be seen as a formal grammar [5]–[7] and the plan verification problem is then similar to checking if a word (action sequence) belongs to the language generated by the grammar, which can be done by parsing. Parsing does not require information about the goal task – the method finds any task that decomposes to the action sequence, which makes it appropriate also for plan and task recognition [8].

The parsing-based approach seems to be significantly faster than the SAT-based approach [4]. Nevertheless, both approaches struggle from the combinatorial explosion and, depending on the domain; they can verify plans of lengths up to a few dozens of actions. This is not surprising as the problem of verifying hierarchical plans is NP-hard [9], [10] and hence computationally expensive. This holds for general hierarchical plans with task interleaving and the partial order of tasks. However, as can be seen from the International Planning

Competition 2020 on HTN planning, many domain models contain totally-ordered tasks. Further, there is a significant body of research dedicated to totally-ordered HTN planning in particular [11]–[20]. Reasoning about totally ordered plans is computationally at most as hard as reasoning about totally ordered ones (and often much easier), which is due to limited interaction of actions/tasks. This is both the case in hierarchical as well as in non-hierarchical planning [21]–[24]. Plan verification is no exception: Verifying a totally-ordered problem without state constraints is known to be tractable, whereas its partially ordered counter-part is still NP-hard [9]. Nevertheless, no hierarchical plan verifier exploits this theoretical result, and no generalisation to problems with state constraints exists.

We propose an extension of the parsing-based verification algorithm [4] to work faster for totally-ordered domain models. While the CYK algorithm [25] for parsing context-free grammars appears to be applicable here at first glance, this is not the case. Totally-ordered models can contain state constraints, which cannot, to our current knowledge, be compiled or handled by the CYK algorithm. Our primary modification is in handling precedence relations in the totally-ordered setting. The extended algorithm still works for arbitrary partially ordered hierarchical plans. It detects if the model uses totally-ordered tasks, and then uses a more strict formulation of precedence constraints, which decreases the number of generated tasks significantly. The algorithm works in a bottom-up fashion starting with a given action sequence  $\bar{a}$ . It terminates once a compound task is found that can be decomposed into  $\bar{a}$ . Apart from other work on plan verification, our approach is loosely related to another that aims at computing abstract plans that are maximally abstract while still allowing to generate a non-redundant plan [26]. The proposed algorithm also performs a bottom-up approach, though it requires a specific decomposition rather than the entire model.

## HTN PLAN VERIFICATION BY PARSING

We use the STRIPS model of actions [27] based on propositional logic. Let  $P$  be a set of propositions describing properties of world states. Then, a world state is modeled as a set  $S \subseteq P$  of propositions that are true in that state (every other proposition is false). Each action  $a$  is modeled by three sets of propositions ( $\text{pre}(a)$ ,  $\text{eff}^+(a)$ ,  $\text{eff}^-(a)$ ), where  $\text{pre}(a)$ ,  $\text{eff}^+(a)$ ,  $\text{eff}^-(a) \subseteq P$  and  $\text{eff}^+(a) \cap \text{eff}^-(a) = \emptyset$ .

The set  $\text{pre}(a)$  describes positive preconditions of action  $a$ . These propositions must be true right before the action  $a$ . Action  $a$  is applicable to state  $S$  iff  $\text{pre}(a) \subseteq S$ . Sets  $\text{eff}^+(a)$  and  $\text{eff}^-(a)$  describe the positive and negative effects of action  $a$ . These propositions will become true or false in the state right after executing the action  $a$ . If an action  $a$  is applicable to state  $S$  then the state right after the action  $a$  is:

$$\gamma(S, a) = (S \setminus \text{eff}^-(a)) \cup \text{eff}^+(a).$$

$\gamma(S, a)$  is undefined if action  $a$  is not applicable to state  $S$ . We say that an action sequence  $(a_1, \dots, a_n)$  is *executable* with respect to a given initial state  $S_0$  if the precondition of each action is satisfied in the state right before it:

$$\text{pre}(a_i) \subseteq \gamma(\gamma(\dots \gamma(S_0, a_1), \dots), a_{i-1}).$$

Hierarchical Task Network Planning [23] was proposed as a planning framework that includes control knowledge as recipes for solving specific tasks. The recipe is modeled using a task network – a set of sub-tasks to solve the task and a set (a conjunction) of constraints between the sub-tasks. Let  $T$  be a compound task and  $(\{T_1, \dots, T_k\}, C)$  be a task network, where  $C$  are its constraints (see later). We can describe the decomposition method as a rewriting rule saying that  $T$  decomposes to sub-tasks  $T_1, \dots, T_k$  under the constraints  $C$ :

$$T \rightarrow T_1, \dots, T_k \ [C]$$

The order of sub-tasks in the rule does not matter (opposite to rewriting rules in grammars) as the precedence constraints in  $C$  explicitly describe the order. If the tasks  $T_1, \dots, T_k$  in each method are totally ordered, then we speak about a *totally-ordered HTN model*.

HTN planning problems are specified by an initial state  $S_0$  and an initial task representing the goal. This goal task needs to be decomposed via decomposition methods until a set of primitive tasks – actions – is obtained. These actions must be totally ordered and satisfy all the constraints obtained during decompositions. The obtained plan  $(a_1, \dots, a_n)$  must be executable with respect to  $S_0$ . The state right after the action  $a_i$  is denoted  $S_i$ . We denote the set of actions to which a task  $T$  decomposes as  $\text{act}(T)$ . If  $U$  is a set of tasks, we define  $\text{act}(U) = \cup_{T \in U} \text{act}(T)$ . The index of the first action in the decomposition of  $T$  is denoted  $\text{start}(T)$ , that is,  $\text{start}(T) = \min\{i | a_i \in \text{act}(T)\}$ . Similarly,  $\text{end}(T)$  means the index of the last action in the decomposition of  $T$ , that is,  $\text{end}(T) = \max\{i | a_i \in \text{act}(T)\}$ .

The decomposition constraints for a method  $T \rightarrow T_1, \dots, T_k$  can be of the following three types, where the first is also known as an ordering constraint and the latter two are essentially state constraints  $(U, V, \{t_1, t_2\} \subseteq \{T_1, \dots, T_k\})$ :

- $t_1 \prec t_2$ : a precedence constraint meaning that in every plan the last action obtained from task  $t_1$  is before the first action obtained from task  $t_2$ ,  $\text{end}(t_1) < \text{start}(t_2)$ ,
- $\text{before}(p, U)$ : a precondition constraint meaning that in every plan the proposition  $p$  holds in the state right before the first action obtained from tasks  $U$ ,  $p \in S_{\text{start}(U)-1}$ ,

- $\text{between}(U, p, V)$ : a prevailing constraint meaning that in every plan the proposition  $p$  holds in all the states between the last action obtained from tasks  $U$  and the first action obtained from tasks  $V$ ,  
 $\forall i \in \{\text{end}(U), \dots, \text{start}(V) - 1\}, p \in S_i$ .

The *HTN plan verification problem* is formulated as follows: Given a sequence of actions  $(a_1, a_2, \dots, a_n)$  and an initial state  $S_0$ , is the sequence of actions executable with respect to  $S_0$  and obtained from some compound task?

Algorithm 1 presents the recent parsing-based approach to HTN plan verification [4] extended with the check of total-order constraints at line 13 (see the next section). The set  $\prec$  represents the precedence constraints of the method,  $\text{bef}$  is the set of *before* constraints, and  $\text{btw}$  is the set of *between* constraints. Executability of the action sequence is verified at lines 2-5. The `while` loop (lines 7-26) groups actions/tasks into compound tasks by using the methods from the model until it finds a task  $T_0$  such that  $\text{act}(T_0) = \{a_1, a_2, \dots, a_n\}$  (line 26, the plan is valid) or it constructs all possible tasks that decompose to a subset of actions in the plan (line 27, the plan is invalid). The sets  $\text{act}(T)$  are represented using Boolean vectors  $I$  ( $I(j) = 1 \Leftrightarrow a_j \in \text{act}(T)$ ). These vectors are used to check that each action is generated from one task only (line 19). Indexes  $b_j$  and  $e_j$  for task  $T_j$  describe values  $\text{start}(T_j)$  and  $\text{end}(T_j)$  respectively. They are used when checking the decomposition constraints.

## TOTALLY-ORDERED HTNS

The parsing-based verification algorithm may generate an exponential number of pairs  $(T, \text{act}(T))$ , where  $T$  is a task and  $\text{act}(T)$  is a subset of actions from the plan that can be generated from the task  $T$ . This is because actions from different tasks may interleave in the plan, and hence we must assume subsets  $\text{act}(T)$  of actions from the plan when composing the tasks  $T$ . There is an exponential number of such sets with respect to the length of the plan. However, when the domain model is totally ordered, then the sets  $\text{act}(T)$  form contiguous sub-sequences of actions (Figure 1).

**Proposition 1.** *For a totally ordered HTN domain model, each task decomposes to a contiguous sub-sequence of actions in the plan.*

*Proof:* Assume a pair of different tasks  $T$  and  $T'$  used in the decomposition of some goal task  $T_g$  to a sequence of actions such that  $T$  and  $T'$  are not descendants of each other. There must exist a common ancestor task  $T_a$  for tasks  $T$  and  $T'$  in the decomposition tree and a method  $T_a \rightarrow T_1, \dots, T_k \ [C]$  used for the decomposition. Let the task  $T$  be obtained from the sub-task  $T_i$  and  $T'$  be obtained from the sub-task  $T_j$ . As the domain model is totally-ordered, without loss of generality, we may assume that  $T_i \prec T_j$  and hence  $\text{end}(T_i) < \text{start}(T_j)$ . As  $T$  is a sub-task of  $T_i$ , we know  $\text{end}(T) \leq \text{end}(T_i)$  and similarly  $\text{start}(T_j) \leq \text{start}(T')$ . Together we get  $\text{end}(T) < \text{start}(T')$ . Hence for any pair of non descendant tasks  $T$  and  $T'$ , it holds either  $\text{end}(T) < \text{start}(T')$

or  $end(T') < start(T)$ , which means that the tasks do not interleave in the plan. ■

We can exploit this property when verifying plans for totally-ordered domain models as follows. Assume a decomposition method  $T \rightarrow T_1, \dots, T_k$  [C] in a totally-ordered domain model. Then it holds  $\forall i \in \{1, \dots, k-1\} : T_i \prec T_{i+1}$ . We call these precedence constraints *direct precedences* to distinguish them from classical precedence relations. Note that it is easy to detect automatically, if the domain model is totally ordered, for example, by using a transitive closure of precedence relations in the decomposition methods and verifying that sub-tasks in the method are totally ordered. The

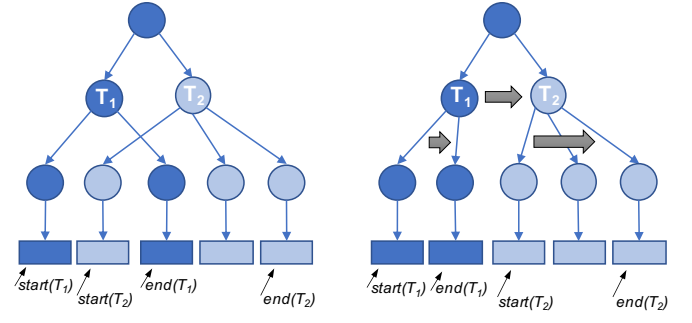


Fig. 1. Task interleaving (left) vs. totally ordered (right).

direct precedence relation  $T_i \prec T_{i+1}$  means that the last action of task  $T_i$  is right before the first action of task  $T_{i+1}$ . This is a consequence of Proposition 1. Task  $T$  decomposes to a contiguous action sequence  $P$ . Each of its sub-tasks  $T_i$  also decomposes to a contiguous action sequence and these sub-sequences are ordered as  $end(T_i) < start(T_{i+1})$ . Together these sub-sequences must form the sequence  $P$  without any gap. Hence, the direct precedence relation imposes a more strict constraint

$$end(T_i) + 1 = start(T_{i+1}). \quad (1)$$

Note that the above claim also holds in the reverse order. Suppose we impose the above ordering constraint (1) for direct precedence relations in all decomposition methods. In that case, the tasks decompose to contiguous sequences of actions as no action can be inserted between any pair of directly following tasks.

The extended HTN plan verification algorithm (Algorithm 1) checks the direct precedence constraints for totally-ordered domain models at line 13. This extension gives the theoretical guarantee on the number of generated tasks.

**Proposition 2.** Let  $t$  be the number of tasks in the totally-ordered HTN domain model and  $n$  be the number of actions in a plan. Then the extended HTN plan verification algorithm generates at most  $O(t \times n^2)$  different pairs  $(T, act(T))$ .

*Proof:* For totally ordered domain models, the sets  $act(T)$  form contiguous sub-sequences of the plan. These sub-sequences are identified by the first and the last actions in the sequence, and hence there are at most  $O(n^2)$  such sets. The same set of actions may be generated from different tasks; hence the maximal number of different pairs  $(T, act(T))$  that the parsing-based verification algorithm may generate is  $O(t \times n^2)$ . ■

Note that if the original verification algorithm is applied to totally-ordered domain models, then it may still generate an exponential number of pairs  $(T, act(T))$  because the algorithm allows sets  $act(T)$  to be arbitrary subsets of actions in the plan. The experimental study confirms this.

## EMPIRICAL EVALUATION

We compared the recent HTN plan verification algorithm [4] with its extended version that detects totally-ordered domain

**Data:** a plan  $P = (a_1, \dots, a_n)$ , an initial state  $S_0$ , and a set of decomposition methods (domain model);  
**TO** = true if the domain is totally ordered,  
**Result:** true if the plan can be derived from some compound task, false otherwise

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1 Function VERIFYPLAN
2   for  $i = 1$  to  $n$  do
3     if  $\neg(pre(a_i) \subseteq S_{i-1})$  then
4       return false
5      $S_i = (S_{i-1} \setminus eff^-(a_i)) \cup eff^+(a_i)$ 
6      $sp \leftarrow \emptyset$ ;  $new \leftarrow \{(A_i, i, i, I_i) \mid i \in 1..n\}$ 
7     Data:  $A_i$  is a primitive task corresponding to action  $a_i$ ,  $I_i$  is a Boolean vector of size  $n$ , such that  $\forall i \in 1..n, I_i(i) = 1, \forall j \neq i, I_i(j) = 0$ 
8     while  $new \neq \emptyset$  do
9        $sp \leftarrow sp \cup new$ ;  $new \leftarrow \emptyset$ 
10      foreach decomposition method  $R$  of the form  $T_0 \rightarrow T_1, \dots, T_k$  [ $\prec, bef, btw$ ] such that  $\{(T_j, b_j, e_j, I_j) \mid j \in 1..k\} \subseteq sp$  do
11        if  $\exists(i, j) \in \prec : \neg(e_i < b_j)$  then
12          continue with the next method
13        if  $TO \wedge \exists i : \neg(e_i + 1 = b_{i+1})$  then
14          continue with the next method
15         $b_0 \leftarrow \min\{b_j \mid j \in 1..k\}$ 
16         $e_0 \leftarrow \max\{e_j \mid j \in 1..k\}$ 
17        for  $i = 1$  to  $n$  do
18           $I_0(i) \leftarrow \sum_{j=1}^k I_j(i)$ ;
19          if  $I_0(i) > 1$  then
20            continue with the next method
21          if  $\exists(p, U) \in bef : p \notin S_{\min\{b_j \mid j \in U\} - 1}$  then
22            continue with the next method
23          if  $\exists(U, p, V) \in btw \exists i \in \max\{e_j \mid j \in U\}, \dots, \min\{b_j \mid j \in V\} - 1 : p \notin S_i$  then
24            continue with the next method
25           $new \leftarrow new \cup \{(T_0, b_0, e_0, I_0)\}$ 
26          if  $\forall k, I_0(k) = 1$  then
27            return true
28      return false

```

Algorithm 1: Parsing-based HTN plan verification

models and imposes constraints (1) to check the direct precedence constraints used in decomposition methods. Compared to previous evaluations, we significantly increased the number of considered instances. The International Planning Competition (IPC) 2020 has released an extensive set of plans<sup>1</sup> that were generated by the planners in the IPC on the IPC domains<sup>2</sup>. We are using the set of totally-ordered plans provided by the IPC, that is, all plans in our evaluation are totally-ordered. This set contains 10963 plans with an average length of 239 actions and a maximum length of 131071 actions.

Both the original verifier [4] and the modifications presented in this paper were implemented in C# 7 (from .NET 4.7). For running the program, we used mono in version 6.8.0.105 on a singularity container based on Ubuntu 20.10. We ran all experiments on an Intel Xeon Gold 6242 CPU (2.80GHz) with 5GB of RAM and a timeout of 10 minutes. The memory limit was never reached.

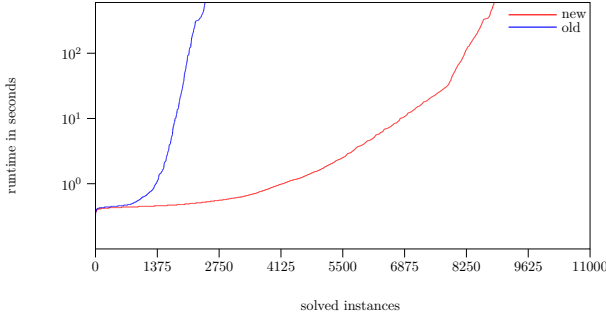


Fig. 2. The number of solved problems per time.

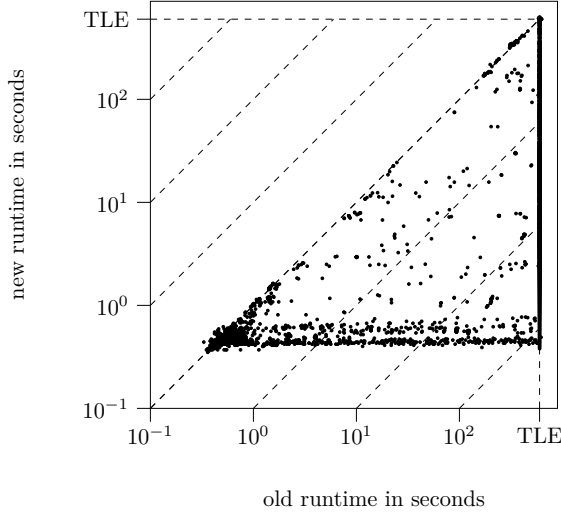


Fig. 3. Direct comparison of runtimes.

The summary results are presented in Figure 2 showing the number of solved instances within a given time. The new approach solves a significantly larger number of instances

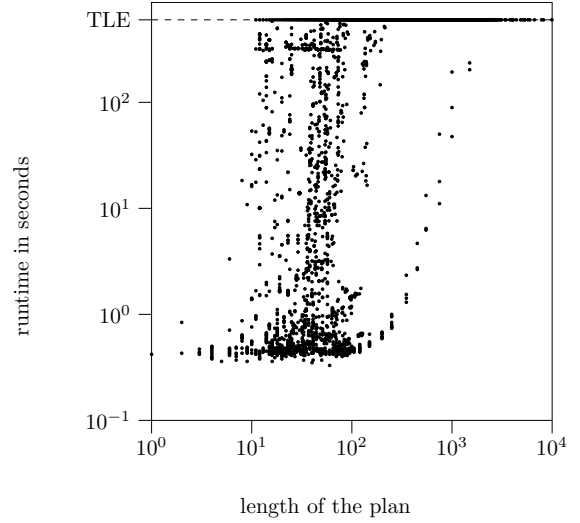


Fig. 4. Runtime of the original algorithm as a function of plan length. Plans with more than 10,000 actions were omitted.

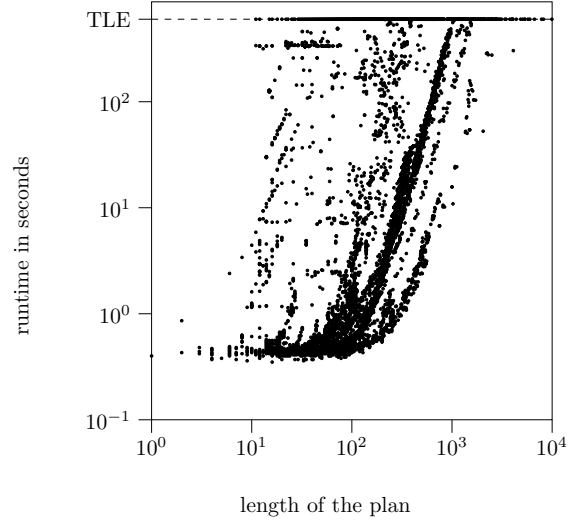


Fig. 5. Runtime of the extended algorithm as a function of plan length. Plans with more than 10,000 actions were omitted.

(8870) than the original approach (2443). Any instance solved by the original approach was also solved by the new approach, while the new approach solved 6427 instances more. Figure 3 presents the direct comparison of both techniques using the same data. Each point represents one of the 2443 problem instances solved by both approaches. The runtimes of the algorithms define the coordinates of the point. Of these 2443 instances, the old approach is faster in 362 instances. Of these 362, only 159 have a runtime of more than one second. For these 362 instances, the old algorithm is faster than the new one by more than 10% in only 24 instances and at the most only 25% faster. The minor overhead of the new algorithm seems not to incur a significant disadvantage. For 210 instances, the runtime is identical, and for the remaining 1871 instances solved by both verifiers, the runtime of the new

<sup>1</sup><https://github.com/panda-planner-dev/ipc-2020-plans>

<sup>2</sup><https://github.com/panda-planner-dev/ipc2020-domains>

one is faster. The reduction in runtime on these 1871 instances is on average 46.36% with a maximum of 99.93%.

Figures 4 and 5 show the dependence of runtime on plan length for the original and extended algorithm, respectively. Again, it is clearly visible that the new method solves a larger number of instances. The new approach can verify about one order of magnitude longer plans than the original algorithm. The longest verified plan for the old technique has 1500 actions, while for the new one has 4095 actions.

## CONCLUSIONS

We proposed extending the HTN plan verification algorithm to impose a more strict constraint describing direct precedence relations for totally-ordered models. The effect of this modification on the runtime of the algorithm is dramatic. The new algorithm verifies a much larger number of problem instances and also longer plans. As totally-ordered HTN domain models are frequent in practical applications, the method brings automated HTN plan verification closer to practical applicability on non-trivial plans and domains.

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